⁶P_{7/2}-Excited-State Decay Mechanism and Energy-Transfer Processes in KMgF₃:Eu²⁺ and $KMgF_3:Eu-X$ (X = Gd, Ce, Cr)

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A four-level decay model in KMgF₃: Eu^{2+} is proposed. The decay profiles of the ${}^{6}P_{7/2}$ excited state of Eu^{2+} are biexponential, and the physical implication of each term in the fit equation responsible for the model is interpreted. The evidence obtained spectroscopically for supporting the model is presented. A new method to study energy transfer between Eu²⁺ and X^{3+} in KMgF₃:Eu-X (X = Gd, Ce, Cr) is established on the basis of the proposed model.

I. Introduction

Optical transitions of divalent europium (4f⁷) ions in $KMgF_3$ have been investigated extensively in many papers¹⁻¹² due to the potential applications for phosphores or lasers.^{13–17} Ellens et al.,³ Francini and coworkers,² and Tsuboi et al.¹ suggest the existence of different possible sites for the impurity in KMgF₃. Although the majority of the divalent europium ions enter substitutionally in the crystal at a cubic site, other lattice sites of lower symmetry are available to europium, i.e., the tetragonal and trigonal symmetries. It is now well established that the presence of broad-band or line emission for Eu²⁺ depends on the coordination number, covalency, and crystal field strength at the Eu^{2+} site. Hence, the position of the 4f⁶5d state can be adjusted by changing the surrounding conditions of the

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 Eu^{2+} ion. It was found that the $^6\ensuremath{P_{7/2}}$ state is at lower energy than the lowest 4f⁶5d state in KMgF₃:Eu²⁺. However, the reported energy differences between the two states vary from author to author. Sardar et al.⁵ estimated the value of 1250 cm⁻¹ from a semilog plot of the ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$ and $4f^65d \rightarrow {}^8S_{7/2}$ emission intensities versus T^{-1} . Altshuler et al.¹² found the value of 120 cm⁻¹ from a fit to the temperature dependence of the ${}^{6}P_{7/2}$ decay time. Ellens and co-workers³ obtained the value of 3350 cm⁻¹ from spectral data and a fit to a threelevel model involving ⁸S_{7/2}, ⁶I_{7/2} and 4f⁶5d levels. They also suggested that the main reason for the erroneous result for $\Delta E_{\rm fd}$ (the energy difference between the lowest $4f^{6}5d$ level and the ${}^{6}P_{7/2}$ level, vide infra) for Eu^{2+} in the former two cases was that the results are fit to a three-level model including the ⁶P_{7/2}, 4f⁶5d, and the ⁸S_{7/2} levels. In reality more levels (6P5/2, 6P3/2, and different 4f⁶5d levels) are involved. In the simple three-level model, the temperature dependence of the ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$ transition probability (Wf in eq 2, vide infra), due to a change in the vibronic transition probability with temperature, is not taken into account. Hence, the values for $\Delta E_{\rm fd}$ from fits to a three-level model are inaccurate. The spectroscopically determined values for $\Delta E_{\rm fd}$ - $(4f^{6}5d^{-6}P_{7/2})$ are more accurate.

Recently we have begun to study the reason for this erroneous value of $\Delta E_{\rm fd}$. Several single crystals of KMgF₃:Eu-X (X = Gd, Ce, Cr) and KMgF₃:Eu²⁺ have been grown in our laboratory, and various optical measurements have been made. On the basis of the temperature dependence of lifetime, we propose a four-level decay model and a biexponential decay equation. Good agreement is found between the fit and the spectroscopic results. On the basis of this four-level model, many optical transition characteristics in KMgF₃:Eu²⁺ can be interpreted, and the energy transfer between Eu^{2+} and other impurities in the codoped KMgF₃ system can be studied more efficiently.

II. Experimental Section

The crystals were grown by the vertical Bridgman method in graphite crucibles in an argon atmosphere. Europium, cerium, chromium, and gadolinium ions were added as EuF₃, CeF₃, Cr₂O₃ and GdF₃, respectively, in stoichiometric mixtures of KF and MgF₂ dehydrated powders. The concentration of the dopant in the melt varied in the range of 0.1-1.0 mol %. The crystals were transparent. Polished pieces of $5 \times 6 \times 7$ mm size were used for the measurements. Previous experiments showed that doping $KMgF_{3}$ with Eu^{3+} ions is extremely difficult if the crystal growth is not carried out in an oxidizing atmosphere.¹⁸ This is evidently caused by a quantitative reduction process to Eu²⁺ ions during the incorporation in the perovskite lattice, which contains practically only divalent ions of the dopant. In the present study, we used crystals grown from a melt containing 1.0 mol % Eu^{2+} ions, which is sufficiently doped to observe the weak $f^7 \rightarrow f^7$ absorption bands. Our absorption and emission spectra showed that the crystals did not contain Eu³⁺ ions.

Absorption spectra were obtained with a model 8452A diode array spectrophotometer. High-resolution emission spectra were recorded using a Spex model 1403 double monochromator equipped with a Spex model DM1B controller and a Hamamatsu R928 photomultiplier tube. Excitation wavelengths at 356.4, 350.9, and 337.5 nm were provided by a coherent model Innova-100-K3 krypton ion laser. Excitation at 354.5 nm was obtained from the third harmonic of a Quanta-Ray (Spectra-Physics) model DCR-3 Nd:YAG laser (operated at 20 Hz).

For lifetime measurements, a frequency-doubled dye laser (Lambda Physik Scanmate 2E) operating on rhodamine 101 dye and pumped by the second harmonic of a Nd:YAG laser operating at 10 Hz was used as the excitation light source. After frequency doubling, this dye laser generates light pulses of about 3 mJ total energy at a wavelength of 308 nm. The spectral bandwidth is about 0.05 cm⁻¹ (fwhm) in a Gaussian envelope.

The crystal samples were fitted into a cryogenic system (Janis Research) with capabilities of automatic temperature control to measure lifetimes at different temperatures. The fluorescence photons were collected using a CaF_2 lens system and focused onto the entrance slit of a low-dispersion-power monochromator with an estimated resolution of 3 nm, and then focused onto the cathode of a photomultiplier tube (PMT) using a fiber optical assembly.

III. Results and Discussion

A. Four-Level Decay Model and the Derivation of the Fitting Equation. In this section, we will concentrate on the decay pattern of the first excited state of the ⁶P_{7/2} energy level of the Eu²⁺ ion. After excitation into the higher 4f⁶5d manifold, Eu²⁺ experiences a rapid, nonradiative decay to the lowest excited 4f⁷ multiplet, and at low temperature fluorescence is almost entirely emitted from the ⁶P_{7/2} state, the lowest component of the ⁶P_J multiplet. When the temperature is increased, fluorescence has also been observed from the ${}^{6}P_{5/2}$ component.⁷ In general, the electronically excited Eu²⁺ ion in its excited state dissipates the excess energy via internal deactivation processes, which include radiative decay, nonradiative decay, and thermal population to a higher energy level, and via intersystem crossing, which includes electron transfer and energy transfer. Given the fact that the $^6\mathrm{P}_{5/2}$ emission is observable at 77 K,⁷ the ${}^8S_{7/2} \rightarrow {}^6P_{3/2}$ absorption band is not observed due to the selection rule $\Delta J = 0$, 1,¹ and the lowest 4f⁶5d levels are just 100 cm⁻¹ above the 4f⁷



Figure 1. Four-level decay pattern of the ${}^{6}P_{7/2}$ excited state of Eu²⁺ in KMgF₃:Eu²⁺: (dotted arrow) thermal population, (solid arrow) radiative transition, (wavy arrow) intersystem crossing.

(⁶I) multiplets,³ we assume that the ${}^{6}P_{5/2}$ level should be taken into account as a thermal population level upon considering the ${}^{6}P_{7/2}$ decay path. It is reasonable to consider the lowest $4f^{6}5d$ level as a second thermally populated energy level of the ${}^{6}P_{7/2}$ state because all the higher $4f^{6}5d$ excited states rapidly relax to the lowest $4f^{6}5d$ energy level. On the basis of the above analysis, we propose a four-level decay pattern of the ${}^{6}P_{7/2}$ excited state, which is shown in Figure 1.

According to the three-level model, the decay time (τ) of the Eu²⁺ luminescence consisting of 4f–4f line emission and 5d–4f band emission can be described by^{19,20}

$$\tau^{-1} = \frac{w_{\rm f} + (g_{\rm d}/g_{\rm f}) w_{\rm d} \exp(-\Delta E/KT)}{1 + (g_{\rm d}/g_{\rm f}) \exp(-\Delta E/KT)}$$
(1)

where g_d , g_f and w_d , w_f are the degeneracies and radiative probabilities of the lowest 4f⁶5d level and of the lowest excited 4f level, respectively.

According to ref 12 the decay time of the Eu^{2+} emission in KMgF₃ can be described by

$$1/\tau = w_{\rm f} + w_{\rm d} \exp(-\Delta E/KT) \tag{2}$$

This equation follows from eq 1 by using the approximations $g_d = g_f$ and $\exp(-\Delta E' KT) \ll 1$.

For the four-level system, another exponential term is needed, and eq 2 can be rewritten as

$$1/\tau = w_{\rm f} + w_{\rm ff} \exp(-\Delta E_{\rm ff}/KT) + w_{\rm d} \exp(-\Delta E_{\rm fd}/KT)$$
(3)

Deactivation of the $^6P_{7/2}$ emitting states can take place via radiative decay and nonradiative decay. For Eu^{2+}, the probability of nonradiative decay between any of the excited states and the ground state is negligibly small and is neglected, due to the large energy difference (about 28000 cm^{-1}) between the $^8S_{7/2}$ state and the excited state. 24

Thermal activation of the ${}^6P_{5/2}$ state and the lowest $4f^{6}5d$ states leads to the opening of two additional energy dissipation pathways. In eq 3, the deactivation rate constant of the thermally populated $4f^{6}5d$ states is

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Table 1. Lifetime of the ⁶P_{7/2} Emitting State of Eu²⁺ in KMgF₃ at Different Temperatures

Eu ²⁺ (1 mol %)		Eu ²⁺⁻ Gd ³⁺ (1, 0.1 mol %)		Eu ²⁺⁻ Ge ³⁺ (1, 0.1 mol %)		Eu ²⁺⁻ Cr ³⁺ (1, 0.5 mol %)	
<i>T</i> (K)	τ (ms)	<i>T</i> (K)	τ (ms)	<i>T</i> (K)	τ (ms)	<i>T</i> (K)	τ (ms)
87.0	3.49	87.9	3.31	88.8	3.37	88.7	3.53
100.1	3.50	106.6	3.29	102.0	3.29	101.6	3.47
155.0	3.37	150.7	3.19	150.8	3.02	150.4	3.24
203.9	2.99	199.6	2.98	204.7	2.79	199.3	3.05
253.0	2.75	249.0	2.83	250.8	2.70	248.0	2.82
300.2	2.63	300.1	2.63	295.8	2.52	298.5	2.57
367.1	2.22	346.9	2.40	348.5	2.27	350.4	2.31
461.0	1.52	440.1	1.68	438.9	1.61	450.2	1.81
$ \begin{pmatrix} 5 & 5 & 5 \\ 5 & 5 & 4 & 4 \\ 1 & 3 & 3 \end{pmatrix} $	50 00 50 00 50 50 00			Absorption(a.u.)	2.5 2.0 1.5 1.0 0.5 0.0		x30
2	50				200	200 40	
250 0.002 0.004 0.006 0.008 0.010 0.012 T ⁻¹ (K ⁻¹)				Figure	200 8 Absorption s	Wavelength(nm)	v F₀∙Fu²+ at ro

Figure 2. Fitting curve of $KMgF_3:Eu^{2+}$ (1 mol %). The solid circle represents the experimental data. The drawn line is a fit based on eq 3 with $w_{\rm f} = 281 {\rm s}^{-1}$, $w_{\rm ff} = 499 {\rm s}^{-1}$, $w_{\rm d} = 2.8 \times 10^{-1}$ 10⁵ s⁻¹, $\Delta E_{\rm ff} = 324$ cm⁻¹, and $\Delta E_{\rm fd} = 2282$ cm⁻¹.

designated w_d and equals the radiative probabilities of the lowest 4f⁶5d level. $\Delta E_{\rm fd}$ is the energy gap between the lowest $4f^{6}5d$ states and the ${}^{6}P_{7/2}$ emitting states. The deactivation rate constant $(w_{\rm ff})$ is associated with the low-lying ⁶P_{5/2} state, which may be thermally populated as a consequence of the small magnitude of $\Delta E_{\rm ff}$, and its physical implication will be discussed later.

*w*_f represents the rate constant for direct radiative decay of the ⁶P_{7/2} state. On the basis of the literature,³ it should contain contributions from the transition probability of the vibrational states (Stokes and anti-Stokes), and thus, *w*_f in eq 3 consists of two terms:

$$W_{\rm f} = A_{\rm vib} + A_{\rm zp} \tag{4}$$

In eq 4 $A_{\rm vib}$ gives the contribution of the vibronic (vib) transitions to the total radiative transition probability $(w_{\rm f})$ of the excited state ${}^{6}\mathrm{P}_{7/2}$. $A_{\rm zp}$ represents the radiative transition probability of the zero-phonon (zp) line (359.3 nm).

B. Fitting Results and Spectral Data. Table 1 presents the lifetime data in the temperature regime 80-450 K for different samples. Fitting the data of KMgF₃:Eu²⁺(1 mol %) to eq 3, we obtained the related parameters as $w_{\rm f} = 281 \text{ s}^{-1}$, $w_{\rm ff} = 499 \text{ s}^{-1}$, $w_{\rm d} = 2.8 \times$ 10^5 s^{-1} , $\Delta E_{\text{ff}} = 324 \text{ cm}^{-1}$, and $\Delta E_{\text{fd}} = 2282 \text{ cm}^{-1}$. Figure 2 shows that the experimental decay data can be fitted quite well to eq 3. w_d is in good agreement with the reported data 6×10^5 and $8 \times 10^5 \, s^{-1}$ (calculated from the lifetime of 1.2 μ s) for Eu²⁺ 5d–4f transitions.^{6,20}

The absorption spectrum of KMgF₃:Eu²⁺ (1 mol %) at room temperature is shown in Figure 3. The absorption due to the ${}^8S_{7/2} \rightarrow {}^6P_{5/2}$ and ${}^8S_{7/2} \rightarrow {}^6P_{7/2}$ transitions at 354 and 360 nm, respectively, are observed, as reported by Tsuboi et al.¹ From the onset of the 4f⁶5d, $^6P_{7/2}$, and $^6P_{5/2}$ absorption bands, $\Delta E_{\rm ff}$ and $\Delta E_{\rm fd}$ can be



estimated for KMgF₃:Eu²⁺. The values are 324 and 2233 cm⁻¹, respectively. Again, these data are in good agreement with the fitting results.

As can be seen from the absorption results, there are some differences between our data and the reported values for $\Delta E_{\rm fd}$, i.e., 1250 cm⁻¹ by Sardar et al.,⁵ 120 cm⁻¹ by Altshuler et al.,¹² and 3350 cm⁻¹ by Ellens et al.³ What is the reason for this difference? Our detailed study shows that the type of model used in the calculation is one factor. Another important factor that affects the 4f⁶5d level position is the oxygen content in the crystals. Since fluoride possesses the pyrohydrolysis property (interaction with water vapor in the crystal growth process), one can suppose that oxygen-containing impurities in KMgF₃ play a very important role.² As reported in the literature,^{4,11,21} the position of the 4f⁶5d state depends on the covalency and crystal field strength at the Eu²⁺ site. Introducing oxygen into the crystal will increase the covalency and crystal field strength at the Eu²⁺ site. As a result the center of gravity of the 4f⁶5d states is shifted to lower energy. That traces of oxygen impurities exist in our crystals is clearly shown in the absorption spectra (Figure 3) at 204 and 224 nm as reported.^{22,23} Thus, it is reasonable that the value of $\Delta E_{\rm fd}$ from our results is smaller than that reported by Ellens et al.3

Figure 4 illustrates the contributions from each term in eq 3 to the total transition probability. As can be seen, at room temperature, the dominant contribution for the total transition probability is from the ⁶P_{7/2} emission, 27% of the energy is lost via the ${}^{6}P_{5/2}$ decay path, and

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Figure 4. Contributions to the total transition probability $(1/\tau)$ from each term in eq 3. The solid circle represents the percentage of $w_{\rm fr}$ the solid triangle corresponds to the percentage of the $w_{\rm ff} \exp(-\Delta E_{\rm ff}/KT)$ term, and the solid square is the percentage of the term $w_{\rm d} \exp(-\Delta E_{\rm fd}/KT)$. The lines drawn through the data points are a guide to the eye.



Figure 5. Emission spectra of $KMgF_3:Eu^{2+}$ excited with a laser at (a) 356.4 nm at room temperature, (b) 350.9 nm at room temperature, (c) 350.9 nm at 77 K and (d) 337.5 nm at room temperature.

the $4f^{6}5d$ emission can be neglected in this case. With an increase of temperature, the $4f^{6}5d$ emission gradually dominates the spectra, and at 650 K a 77% contribution is from this level and the line emission intensity becomes negligible. This result agrees well with the reported one.⁵

It is important to note how the ${}^6P_{5/2}$ level loses its energy after it is thermally populated. Releasing energy through nonradiative decay to the ⁸S_{7/2} ground state is impossible because of the large energy gap between the ⁶P_{7/2} and ⁸S_{7/2} states. Another possible path is through direct emission, but this possibility is excluded by the fact that the ⁶P_{5/2} emission is not available above 77 K in our crystal. The third possibility is that the ⁶P_{5/2} state thermally populates the 4f⁶5d level. If this is the case, the two exponential decays in eq 3 become unnecessary. On the basis of the above analysis, we conclude that the ⁶P_{5/2} state is a special energy dissipation pathway. The preexponential factor $w_{\rm ff}$ represents the dissipation coefficient. At about 400 K (Figure 4), the energy loss via the ⁶P_{5/2} channel reaches its maximum. Taking into account the thermoluminescence at 390 K described in the literature,^{22,23} we assume that the lost energy is most possibly related to the energy transfer to the F_n color and oxygen centers in the crystal by intersystem crossing. Our emission spectra (see Figure 5) excited with different wavelengths of the UV-laser beam demonstrate the existence of O^{2-} and F_n centers. As de-



Figure 6. Emission spectrum of KMgF₃:Eu²⁺ excited with a 350.9 nm laser at 77 K.

scribed in the literature,^{23,26} a complex emission spectrum consisting of overlapping bands in the range of 370–700 nm is connected with intrinsic point defects and oxygen impurity contents.

An important fact to support the above argument is the intensity ratio of line (360 nm) to band (370-700 nm) emission. At room temperature, the energy loss via the ⁶P_{5/2} state almost reaches its maximum. The $KMgF_3:Eu-X$ (X = Gd, Ce, Cr) codoped system can considerably change the value of $w_{\rm ff}$ (vide infra, Table 4). If energy transfer from the ${}^{6}P_{5/2}$ state to the F_n and oxygen centers exists, then introducing Gd³⁺ and Ce³⁺ will lower the intensity of the F_n and oxygen centers, whereas introducing Cr^{3+} will result in an increase of the intensity of the F_n and oxygen centers. Calculating the ratios of the integral intensities of the line to band emission from emission spectra at room temperature, we found values of 0.20, 0.19, and 0.13 for X = Gd, Ce, and Cr, respectively. The ratio for $KMgF_3:Eu^{2+}$ is 0.15. The order of these ratios is in good agreement with the values expected. We also note that, with a decrease in temperature (Figure 5b,c), the emission intensity of the deep trap (500 nm) and O^{2-} (530 nm) centers increases, whereas the intensity of the emission related to point defects (407, 470, and 580 nm) decreases. At 77 K, no contribution from $^6\mathrm{P}_{5/2}$ can be obtained. As a result, the emission intensity of some point defects decreases or disappears (407 nm).

When the temperature is held at 77 K, there are almost no contributions from ${}^6P_{5/2}$ and $4f^{6}5d$ thermally populated decay. An energy of 99.7% emits radiatively via the ${}^6P_{7/2}$ excited state. Then, the two exponential terms in eq 3 can be neglected, and eq 3 becomes

$$1/\tau = w_{\rm f} = A_{\rm vib} + A_{\rm zp} \tag{5}$$

In eq 5, $A_{\rm vib}$ gives the contribution of the vibronic transitions to the total radiative transition probability ($W_{\rm f}$) of the ${}^{6}\mathrm{P}_{7/2}$ excited state. The ratio of the total vibronic intensity to the total zero-phonon line intensity is given by

$$R = I_{\rm vib} / I_{\rm zp} = A_{\rm vib} / A_{\rm zp} \tag{6}$$

From the *R* value and the decay time, the vibronic and zero-phonon transition probabilities (A_{vib} and A_{zp}) can be obtained by eqs 5 and 6.^{3,24,25} Using the *R* value from

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Table 2. *w*_f Values Obtained from the Fit and Emission Spectra

	w _f (s	-1)		$W_{\rm f}~({ m s}^{-1})$	
sample	fit	calcd	sample	fit	calcd
Eu ²⁺ (1 mol %) Eu ²⁺⁻ Gd ³⁺ (1, 0.1 mol %)	$\begin{array}{c} 281\pm \textbf{2} \\ 300\pm \textbf{1} \end{array}$	287 302	Eu ^{2+–} Ce ³⁺ (1, 0.1 mol %) Eu ^{2+–} Cr ³⁺ (1, 0.5 mol %)	$\begin{array}{c} 304\pm3\\ 283\pm1 \end{array}$	298 282

Table 3. Calculated $\Delta E_{\rm ff}$ and $\Delta E_{\rm fd}$ from Absorption Spectra

sample	$\Delta E_{ m ff}(m cm^{-1})$	$\Delta E_{ m fd}~(m cm^{-1})$
Eu ²⁺⁻ Gd ³⁺ (1, 0.1 mol %)	324	2139
Eu ²⁺⁻ Ce ³⁺ (1, 0.1 mol %)	324	1850
Eu ²⁺⁻ Cr ³⁺ (1, 0.5 mol %)	324	1850

Table 4. Fit Parameters from Eq 3 for Different Crystals

sample	$w_{\rm f}({ m s}^{-1})$	$w_{\mathrm{ff}}(\mathbf{s}^{-1})$	$10^5 W_{fd} (s^{-1})$
Eu ²⁺ (1 mol %)	281	499	2.8
Eu ²⁺⁻ Gd ³⁺ (1, 0.1 mol %)	300	358	2.1
Eu ²⁺⁻ Ce ³⁺ (1, 0.1 mol %)	304	422	0.8
Eu ^{2+–} Cr ³⁺ (1, 0.5 mol %)	283	503	0.4

the emission spectrum (Figure 6) and the lifetime at 77 K, i.e., $\tau = 3.49$ ms and R = 2.2 (integral intensity ratio), we obtained $A_{zp} = 89 \text{ s}^{-1}$ and $A_{vib} = 198 \text{ s}^{-1}$. Thus, $w_f = A_{vib} + A_{zp} = 287 \text{ s}^{-1}$. Similarly, the values of the other crystals can be calculated and are shown in Table 2. As can be seen, all values agree well with those obtained from the fitting result.

Summarizing, the temperature dependence of the lifetime of the Eu²⁺ ⁶P_{7/2} luminescence in KMgF₃:Eu²⁺ and KMgF₃:Eu²⁺⁻X (X = Gd, Ce, Cr) has been measured in the temperature range of 80-460 K. All of the data can be well fit to a biexponential decay equation. A four-level decay model responsible for the fit equation was proposed. The fit results for $\Delta E_{\rm ff}$ and $\Delta E_{\rm fd}$ for KMgF₃:Eu²⁺ are in good agreement with the data obtained spectroscopically. The reason for the $\Delta E_{\rm fd}$ differences from different laboratories is suggested to be differences in the calculation method and oxygen content in the sample. The radiative transition probability of the 4f⁶5d excited state agrees with the reported value. Vibronic and zero-phonon transition probabilities of the ${}^6P_{7/2} \rightarrow {}^8S_{7/2}$ transition of Eu²⁺ in KMgF₃ were calculated. An important energy dissipation pathway from the ⁶P_{5/2} excited state was found, and it is most likely related to the intrinsic point defects and oxygen centers in the crystal.

C. Study of Energy Transfer Using the Four-Level Model in KMgF₃:Eu–X (X = Gd, Ce, Cr). From absorption spectra, $\Delta E_{\rm ff}$ and $\Delta E_{\rm fd}$ can be estimated for three other crystals and are presented in Table 3.

Introducing these data into eq 3 and then fitting the data in Table 1, we obtained all of the parameters, which are shown in Table 4.

Table 4 shows that doping with other impurity ions considerably affects all the transition probability terms in eq 3. Comparing Gd–Eu and Ce–Eu codoped KMgF₃ with KMgF₃:Eu²⁺, we found that $w_{\rm f}$ is increased whereas $w_{\rm ff}$ and $w_{\rm d}$ are decreased. These results clearly indicate that energy transfer from Gd³⁺ and Ce³⁺ to the f–f level of the Eu²⁺ ion takes place in the studied systems. On the other hand, doping the crystal with Cr^{3+–}Eu²⁺ results in almost the same $w_{\rm ff}$ and $w_{\rm ff}$ as those for

KMgF₃:Eu²⁺, which indicates no influence of Cr³⁺ doping on the f–f luminescence (total luminescence of the zero-phonon and vibronic transitions) of the Eu²⁺ ion. However, doping the crystal with Cr^{3+–}Eu²⁺ reduced the 4f⁶5d transition probability by a factor of 7, which implies that energy transfer happens from the ⁶P_{7/2} level of Eu²⁺ to the 3d level of Cr³⁺. It is interesting to note that the 4f⁶5d transition probability (*w*_d) is gradually decreased in the order Gd, Ce, and Cr, which results from d–d interaction between Eu²⁺ and these ions and has been discussed in more detail elsewhere.²⁷

To verify the energy transfer described above, we conducted a series of emission measurements excited at different wavelengths and calculated their relative integral intensity, which is presented in Table 5.

Table 5 shows that doping KMgF₃ with Eu²⁺⁻Gd³⁺ and Eu²⁺⁻Ce³⁺ significantly increases the total intensity (I_t) of the zero-phonon and vibronic transitions of the Eu^{2+} ion. But doping with Cr^{3+} has no effect on the I_t of $KMgF_3:Eu^{2+}$. Thus, the spectral data support the results from the fit. Table 5 also demonstrates that the percentage of zero-phonon transition emission of Eu²⁺ is decreased upon doping $KMgF_3$ with $Eu^{2+-}Gd^{3+}$, $Eu^{2+-}Ce^{3+}$, and $Eu^{2+-}Cr^{3+}$, which implies that the vibronic transition emission (I_{vib}) is increased with the doping of other mentioned ions. These results suggest that energy transfer from Gd³⁺ and Ce³⁺ to Eu²⁺ occurs in KMgF₃:Eu–Gd and KMgF₃:Eu–Ce, but the energy is transferred to the vibronic transition. As described previously, the vibronic transition probability (A_{vib}) and zero-phonon transition probability (A_{zp}) can be calculated from eqs 5 and 6 at 77 K. In fact, at any temperature, the fit parameter $W_{\rm f}$ represents the total contribution from A_{vib} and A_{zp} , but the ratio of A_{vib} to A_{zp} varies with temperature. Therefore, the values of $A_{\rm vib}$ and $A_{\rm zp}$ at any temperature can be calculated on the basis of the emission spectra ($R = I_{vib}/I_{zp}$) and fit parameter ($W_{\rm f} = A_{\rm vib} + A_{\rm zp}$). The calculated results at 77 and 300 K are presented in Table 6. It clearly shows that the energy from Gd³⁺ or Ce³⁺ is transferred to the vibronic transition of Eu²⁺. For the KMgF₃:Eu-Cr system, although the total transition probability $W_{\rm f}$ is the same as that of KMgF₃:Eu²⁺, i.e., no energy transfer from Cr^{3+} to the f-f level of Eu^{2+} , the zero-phonon transition probability is considerably decreased and the vibronic transition probability is increased.

Another interesting result can be drawn from the data of Table 5. When Eu^{2+} is excited at 350.9 nm into its ${}^{6}P_{5/2}$ manifold at 77 K, the total intensity (I_{t}) of KMgF₃:Eu–Gd is two times greater than that of KMgF₃:Eu. At 77 K, the thermal population of ${}^{6}P_{5/2}$ and 4f⁶5d can be neglected (Figure 4), and the only decay path of the ${}^{6}P_{5/2}$ excited state is the relaxation to the ${}^{6}P_{7/2}$ excited state or the direct energy loss through the ${}^{6}P_{5/2}$ pathway. Thus, KMgF₃:Eu²⁺ will lose much more energy than KMgF₃:Eu²⁺⁻Cd³⁺ via the ${}^{6}P_{5/2}$ pathway

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Table 5. Relative Emission Intensity of Zero-Phonon and Vibronic Transitions of Eu²⁺ in Different Crystals

laser excitation	Eu ²⁺ (1 mol %)		Eu ²⁺⁻ Gd ³⁺ (1, 0.1 mol %)		Eu ²⁺⁻ Ce ³⁺ (1, 0.1 mol %)		Eu ^{2+–} Cr ³⁺ (1, 0.5 mol %)	
wavelength (nm)	Ita	Izp ^b (%)	It	Izp (%)	It	Izp (%)	It	<i>I</i> _{zp} (%)
350.9	720	28			1800	24		
350.9 ^c	5800	31	12000	23				
337.5	$6.4 imes10^6$	27			$2.1 imes10^8$	27		
354.5	99	25			102	24	100	23
356.4	590	25			4700	25		

^{*a*} Total intensity of the zero-phonon (360 nm) and vibronic transitions. ^{*b*} Intensity of the zero-phonon transition. $I_{\rm t} = I_{\rm vib} + I_{\rm zp}$. $I_{\rm zp}$ (%) = $I_{\rm zp}/I_{\rm t} \times 100$. ^{*c*} Emission at 77 K.

Table 6. Calculated Vibronic and Zero-Phonon Transition Probabilities from Emission Spectra and the Fit Equation

	300 K		77 K	
sample	A _{vib}	A _{zp}	A _{vib}	Azp
Eu ²⁺ (1 mol %)	203	78	194	87
Eu ²⁺⁻ Gd ³⁺ (1, 0.1 mol %)	224	76	232	67
Eu ²⁺⁻ Ce ³⁺ (1, 0.1 mol %)	230	75	216	89
$Eu^{2+-}Cr^{3+}$ (1, 0.5 mol %)	218	64		

because of the larger $w_{\rm ff}$ value of the former, which results in weaker emission of KMgF₃:Eu²⁺.This result strongly supports the fact that the $^6P_{5/2}$ channel exists in the KMgF₃:Eu–X system.

To summarize, we have described the application of a four-level model in studying the energy transfer between Eu^{2+} and Ce^{3+} , Gd^{3+} in the KMgF₃ host. The energy-transfer mechanism and the energy dissipation path are well explained by this model. Ce^{3+} and Gd^{3+} are good sensitizers for the vibronic transition of Eu^{2+} in KMgF₃.

IV. Conclusion

The temperature dependence of the lifetime of the $Eu^{2+} {}^{6}P_{7/2}$ emission in KMgF₃:Eu–X (X = Gd, Ce, Cr) and KMgF₃:Eu in the range of 80–460 K can be well fit to a biexponential decay equation. A four-level decay model responsible for the fit equation was proposed. On the basis of this model, the energy difference between 4f⁶5d and ${}^{6}P_{7/2}$, ${}^{6}P_{5/2}$ and ${}^{6}P_{7/2}$ can be obtained from the

fit. The reason for the different values of the energy difference between 4f⁶5d and ⁶P_{7/2} with different authors is attributed to differences in the calculation method and oxygen impurity content in the crystal. The 4f⁶5d transition probability and vibronic and zero-phonon transition probabilities of the ⁶P_{7/2} \rightarrow ⁸S_{7/2} transition of Eu²⁺ in KMgF₃ above 77 K can be calculated from fit parameters and emission spectra. An important energy dissipation pathway from the ⁶P_{5/2} excited state was found, and it is most likely related to the intrinsic point defects and oxygen centers in the crystal.

The energy-transfer mechanism in the codoped KMgF₃ system can be studied by the measurement of the temperature dependence of the lifetime on the basis of the four-level decay model. Doping KMgF₃ with $Eu^{2+-}Gd^{3+}$ and $Eu^{2+-}Ce^{3+}$ increases the vibronic transition probability of the ${}^{6}P_{7/2} \rightarrow {}^{8}S_{7/2}$ transition of Eu^{2+} . Introducing $Cr^{3+-}Eu^{2+}$ into KMgF₃ results in a decrease of the zero-phonon transition probability of the Eu^{2+} ion.

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